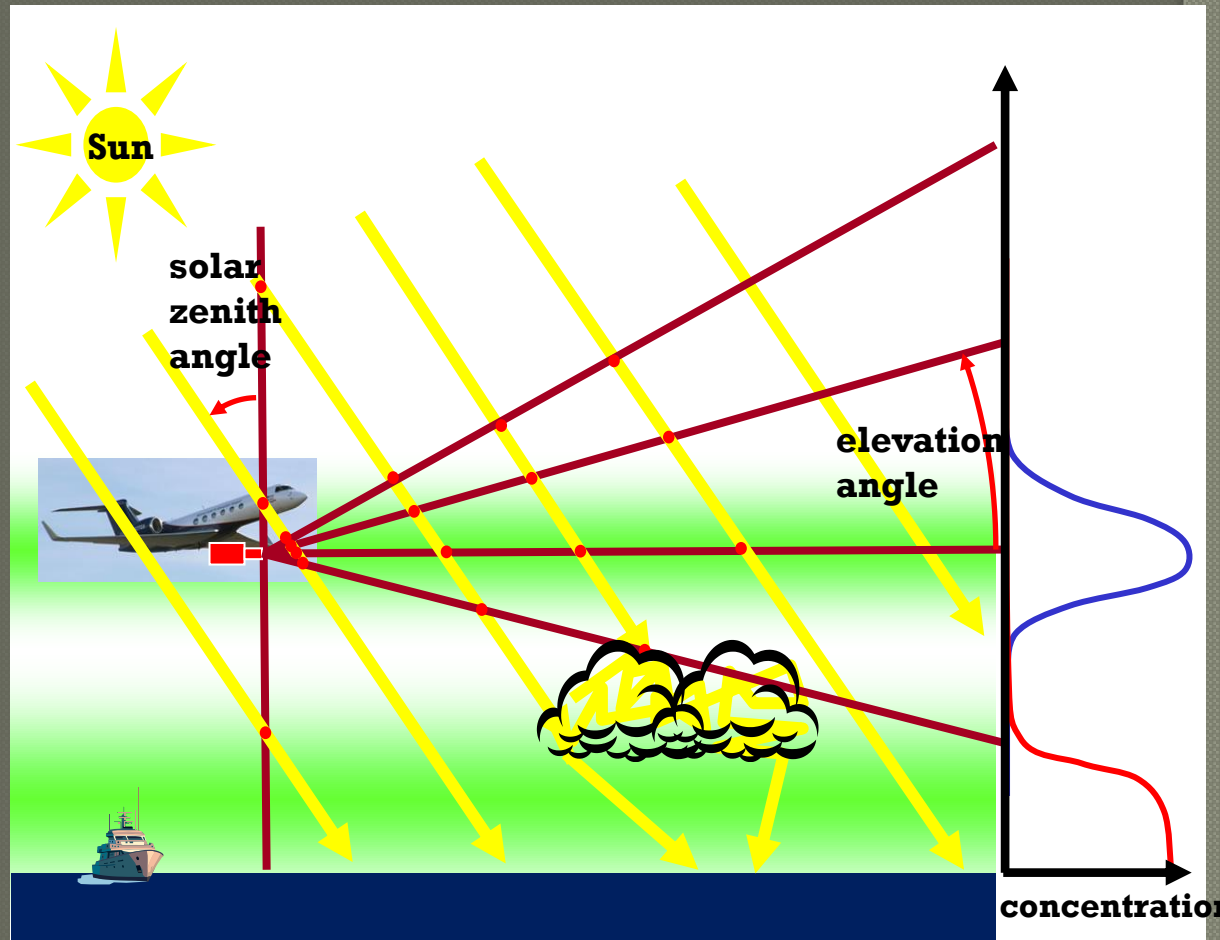


# Inverse modeling to retrieve vertical profiles of aerosol extinction and trace gases

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- Primary quantity measured by AMAX-DOAS is Slant Column Densities (SCDs).
- SCD- Integrated concentration of species along the light path.

- Difficult to interpret.
- Requires knowledge of effective light path
- Radiative transfer program
- Inversion technique



$$\mathbf{y} = \mathbf{F}(\mathbf{x}, \mathbf{b}) + \boldsymbol{\varepsilon}$$

$$\mathbf{y} \approx \mathbf{K}\mathbf{x} + \boldsymbol{\varepsilon}$$

$$\text{where } \mathbf{K} = \frac{\partial \mathbf{F}(\mathbf{x})}{\partial \mathbf{x}}$$

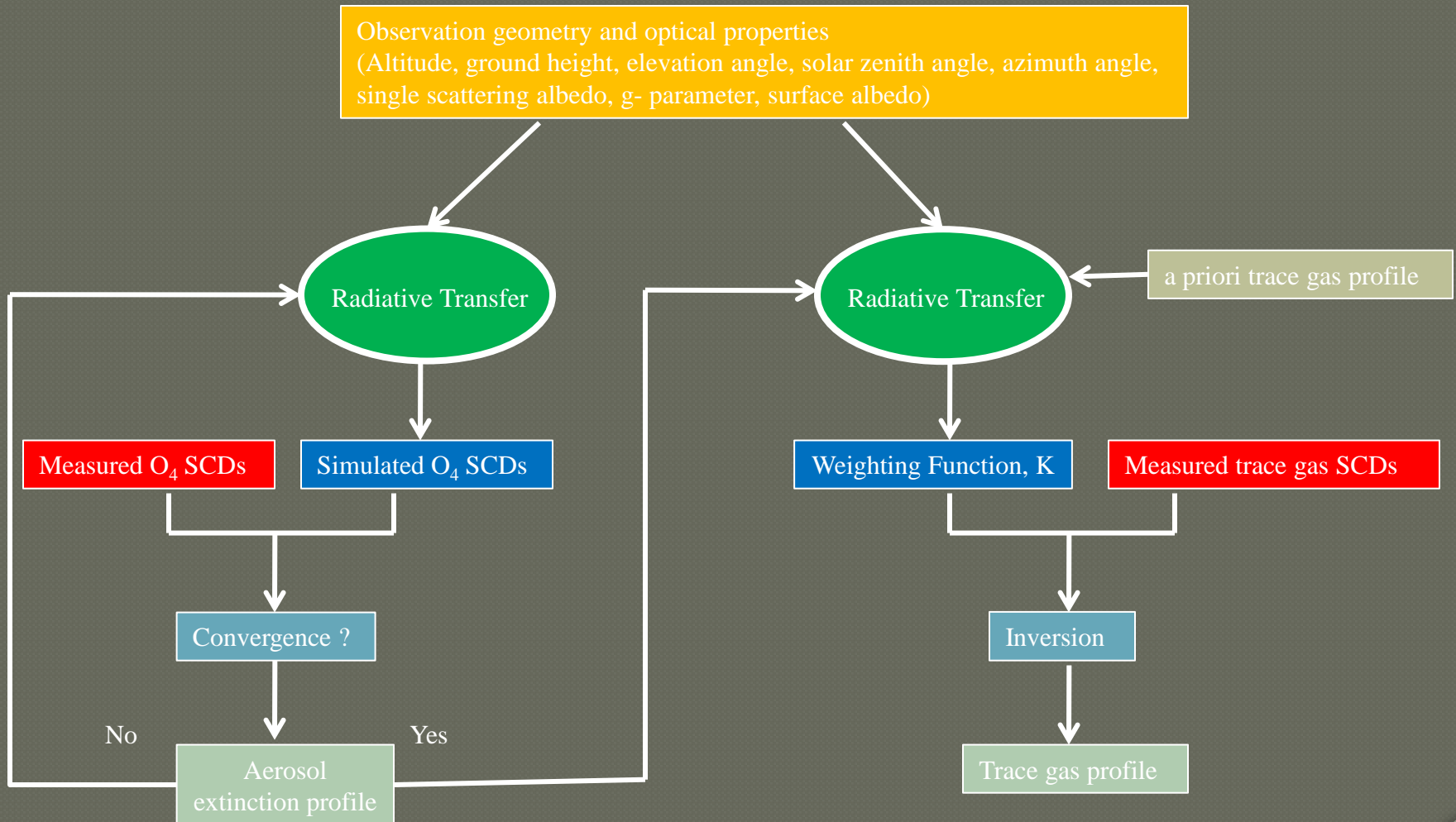
## Optimal Estimation

- Uses a priori profile,  $\mathbf{x}_a$  to constrain the problem.
- provides best solution out of all the possible solutions.

Linear Solution:

$$\hat{\mathbf{x}} = (\mathbf{K}^T \mathbf{S}_{\boldsymbol{\varepsilon}}^{-1} \mathbf{K} + \mathbf{S}_a^{-1})^{-1} (\mathbf{K}^T \mathbf{S}_{\boldsymbol{\varepsilon}}^{-1} \mathbf{y} + \mathbf{S}_a^{-1} \mathbf{x}_a)$$

# Profile retrieval Algorithm



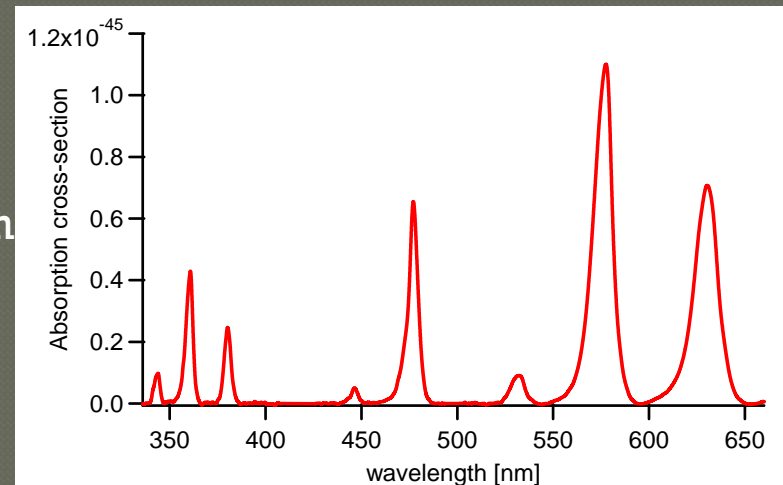
# Aerosol Extinction Profile Retrieval

$O_4$

- $O_2$  dimer
- Concentration of  $O_4$  is well known
  - depends only on temperature, pressure and  $O_2$  concentration
- Any deviation in  $O_4$  scds from the simulated  $O_4$  scds for the Rayleigh atmosphere is due to the extinction of light by aerosols and clouds.
- $O_4$  measurement at 360, 477, 577 and 630 nm.

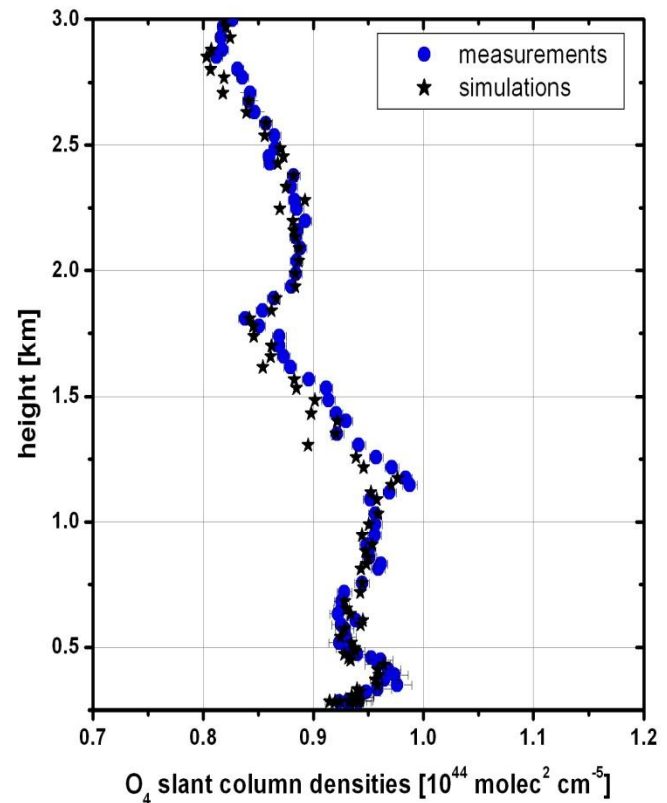
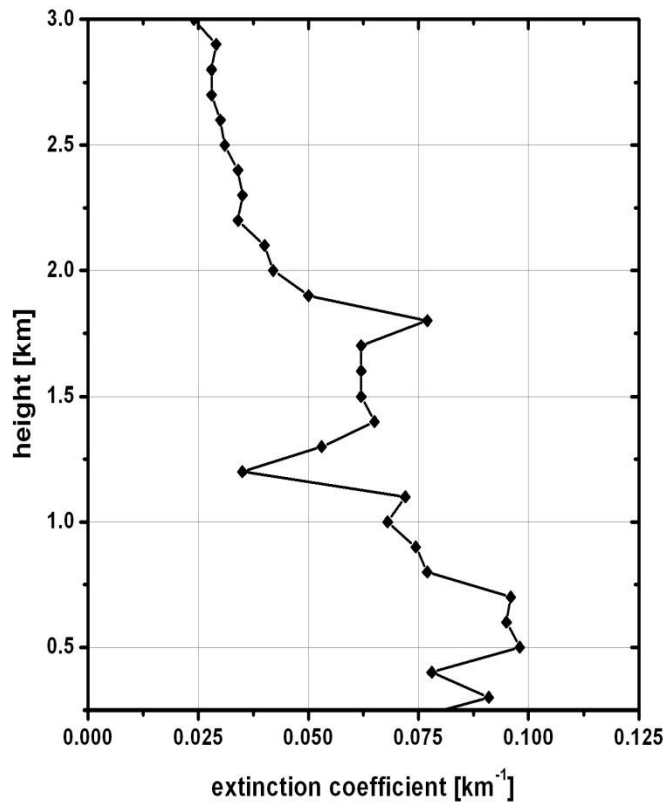
## Radiances

Relative radiance ratio of different  
retrieve aerosol extinction profiles.



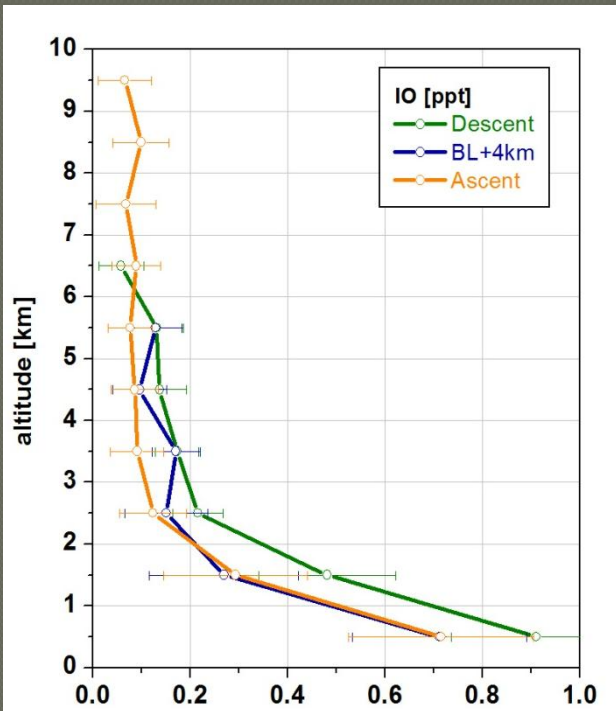
# Example Aerosol Extinction Profile

Only 0 degree elevation angle!

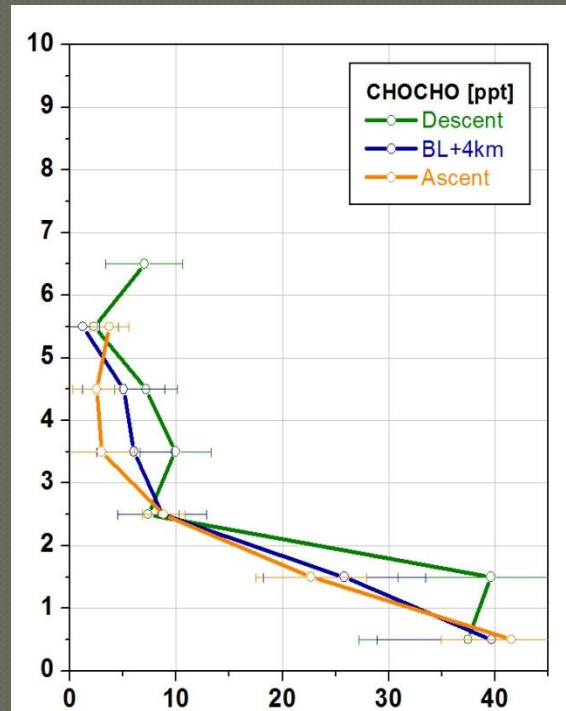


# Example Trace Gas Profiles

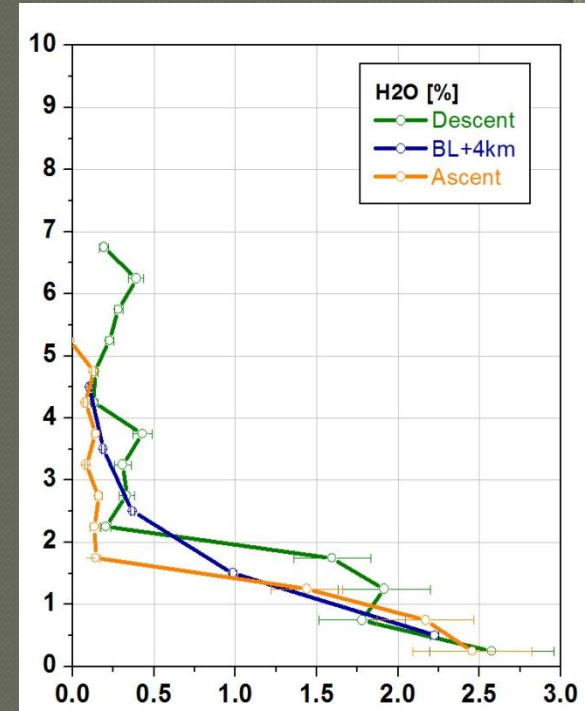
IO

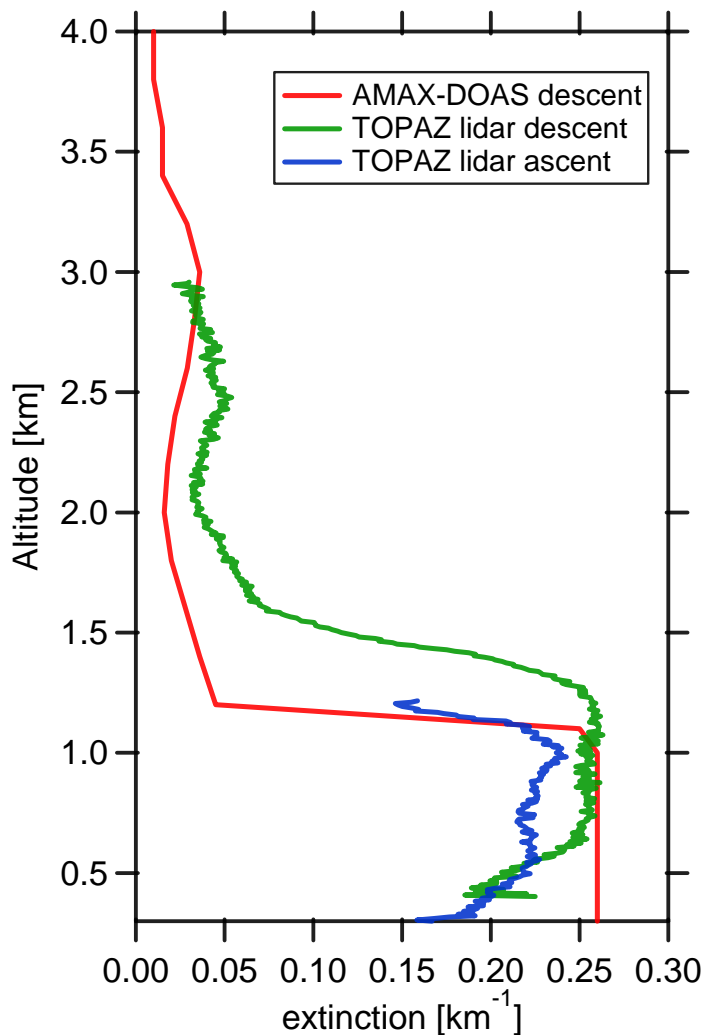


CHOCHO



H<sub>2</sub>O





- Aerosol extinction profile from NOAA TOPAZ lidar and AMAX-DOAS.
- Different air masses being probed by AMAX-DOAS and TOPAZ at a given segment.
- How do we maximize the overlap between different instruments?



Instrument	Species / Parameters	Detection limit / Accuracy / Comment	Time / Space resolution	PI / Institution
CU AMAX-DOAS	IO BrO OCIO NO <sub>2</sub> HCHO CHOCHO	0.1 ppt 1 ppt 0.7 ppt 10 ppt 120 ppt 3 ppt	Acquisition: 2-30 sec Profile scan: 1-5 mins Vertical resolution: ~ few 100 m– few km	Rainer Volkamer (CU Boulder)
HARP	Photon actinic flux: J <sub>O<sub>3</sub></sub> , J <sub>NO<sub>2</sub></sub> , J <sub>OVOC</sub> , J <sub>RX</sub> , J <sub>IxOy</sub> etc. Hyper spectral irradiance Surface albedo Cloud optical depth + Percent cloud cover Cloud/Aerosol eff. radius Single scattering albedo Asymmetry parameter	~ 9 % (280–680 nm)  < 5 % (260–2217 nm) < 3 % ~ 3 %  ~ 5 % ± 0.03 ~ 0.1	0.1 – 3 sec  1 sec inferred by difference from hyper spectral irradiance data	Sam Hall (NCAR/ACD)  Sebastian Schmidt (CU Boulder)
GV-HSRL	Aerosol Backscatter, Depolarization, Extinction altitude profiles	1x10 <sup>-9</sup> m <sup>-1</sup> sr <sup>-1</sup> ~ 1% 2x10 <sup>-8</sup> cm <sup>-1</sup>	Acquisition: 0.5 sec Profile time: 3-5 mins Vertical res.: 7.5 m Range: 30 km	Ed Eloranta (U Wisconsin)
Microwave Temperature Profiler	Altitude temperature profile	1 K (near plane) < 2 K (within 6km from plane)	Profile scan: 18 sec Vertical resolution: ~150 m to few km	Julie Haggerty (NCAR/RAF)

# Discussions

Radiative transfer calculation would be greatly improved by having independent measurement of

1. Temperature Profile (MTP)
2. Aerosol extinction profile (HSRL)
3. Cloud layer altitude (HSRL)
4. Surface albedo (HARP)
5. Aerosol optical depth (HARP)
6. Single scattering albedo, asymmetry parameter (HARP)

## Optimal Estimation:

- formally described by Clive Rodgers (Rodgers, 1976).
- Uses a priori profile,  $\mathbf{x}_a$  to constrain the problem.
- provides best solution out of all the possible solutions.

## Linear Solution:

$$\hat{\mathbf{x}} = (\mathbf{K}^T \mathbf{S}_\varepsilon^{-1} \mathbf{K} + \mathbf{S}_a^{-1})^{-1} (\mathbf{K}^T \mathbf{S}_\varepsilon^{-1} \mathbf{y} + \mathbf{S}_a^{-1} \mathbf{x}_a)$$

$\hat{\mathbf{x}}$  the retrieved state vector

$\mathbf{x}_a$  the a priori information of the state

$\mathbf{S}_a$  the a priori covariance. A square matrix with the uncertainty of the a priori as diagonal elements.

$\mathbf{S}_\varepsilon$  covariance of the uncertainty of the measurement.

$\mathbf{K}$  weighting function matrix.

$\mathbf{S}_a$  is also used as the tuning parameter to maximize the information content while avoiding oscillations.