

# Parameterization of Langmuir turbulence

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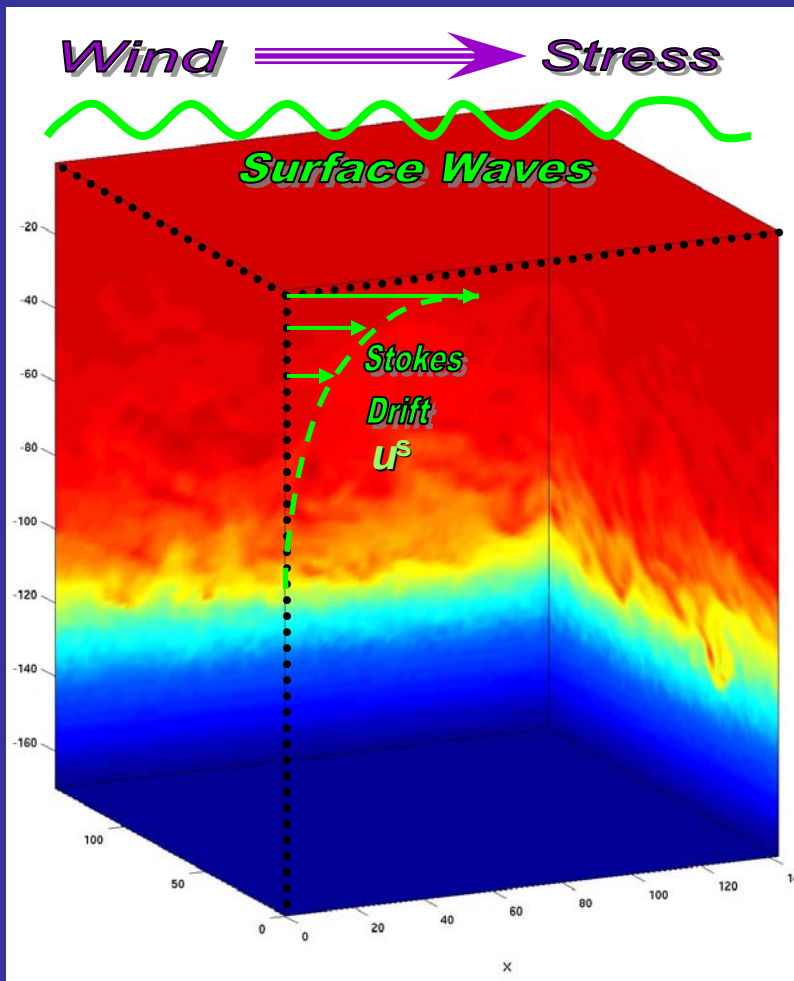
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Support: Typhoon DRI

DoD HPC resources

Collaborator Eric A. D'Asaro



## Methods

1) Modeling upper ocean turbulence with Large Eddy Simulation (LES) techniques

2) Comparing with turbulence observations from Lagrangian floats in wind & wave – driven mixed layers, below & near hurricanes & typhoons.

3) Parameterizing the effects of surface waves on upper ocean turbulence and mixed layer evolution in KPP and in second moment  $q^2$ - $q^2\ell$  type closures (e.g. M-Y 2.5, in NCOM)



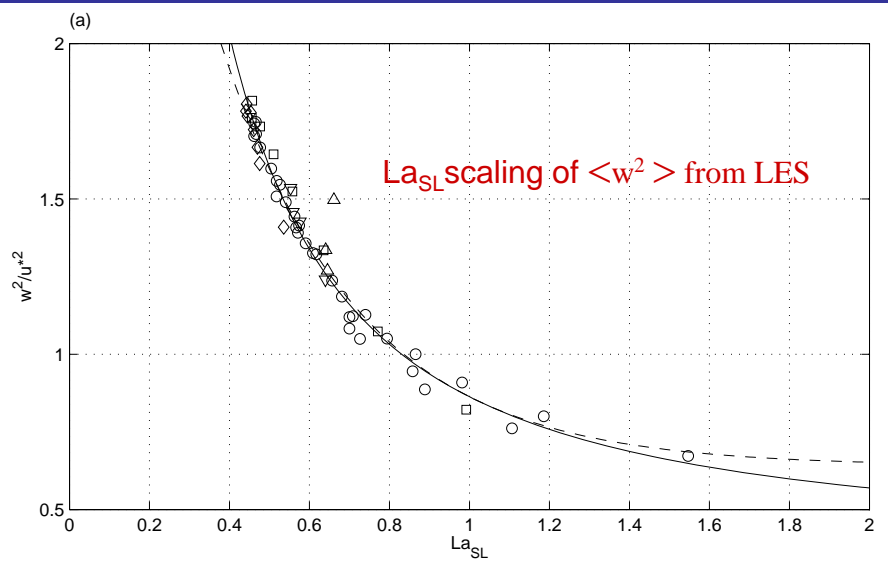
$$\frac{D}{Dt}(q^2) - \frac{\partial}{\partial z} \left[ qlS_q \frac{\partial}{\partial z}(q^2) \right] = -2\overline{uw} \left( \frac{\partial U}{\partial z} + \frac{\partial u_s}{\partial z} \right) - 2\overline{vw} \left( \frac{\partial V}{\partial z} + \frac{\partial v_s}{\partial z} \right) + 2\beta g \overline{w\theta} - 2 \frac{q^3}{B_1 \ell}$$

$$\frac{D}{Dt}(q^2 \ell) - \frac{\partial}{\partial z} \left[ qlS_1 \frac{\partial}{\partial z}(q^2 \ell) \right] = E_1 \ell \left( -\overline{uw} \frac{\partial U}{\partial z} - \overline{vw} \frac{\partial V}{\partial z} \right) + E_6 \ell \left( -\overline{uw} \frac{\partial u_s}{\partial z} - \overline{vw} \frac{\partial v_s}{\partial z} \right)$$

$$+ E_3 \ell_j (\beta g \overline{w\theta}) - E_2 \frac{q^3}{B_1} \left[ 1 + E_4 \left( \frac{\ell}{\kappa \ell_w} \right)^2 \right] + E_5 (2\Omega) q^2 \ell$$

Stokes drift  $u^s$  drives 'vortex force' production in TKE ( $q^2$ ) (McWilliams et al., 1997) and length scale ( $q^2\ell$ ) equations (Kantha & Clayson, 2004)

# Steady State LES of Langmuir turbulence

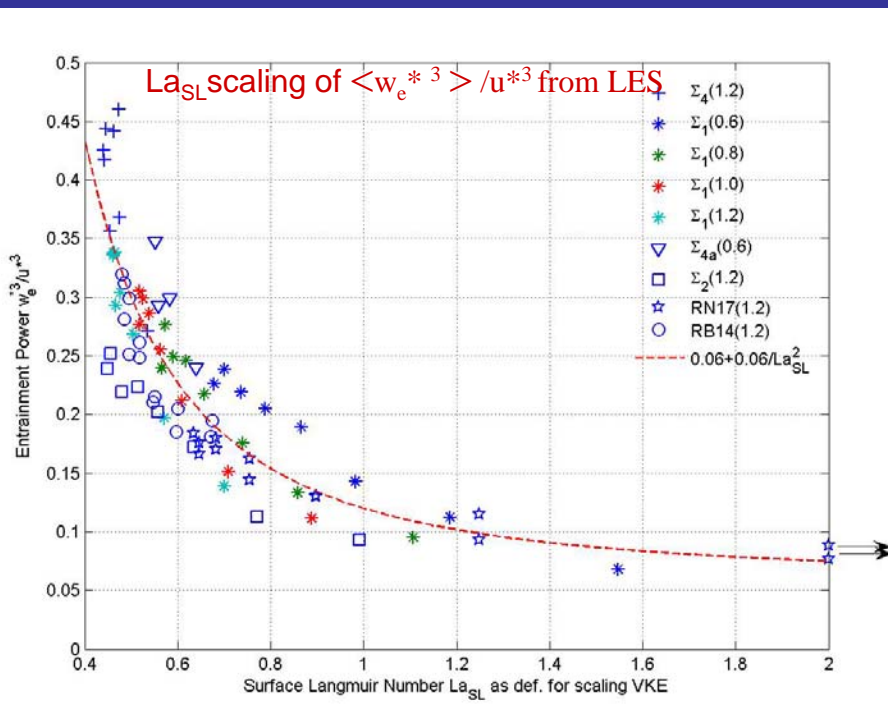


## Scaling of bulk ML Vertical TKE:

Harcourt & D'Asaro (2008):  $\langle w^2 \rangle / u^{*2} \sim La_{SL}^{-4/3}$

Uses a 'Surface Layer Langmuir Number  $La_{SL}$  using near-surface mean  $\langle u^s \rangle$ .

Consistent Lagrangian float  $\langle w^2 \rangle$  observations.



## Scaling entrainment power:

Energy rate to entrainment  $\langle w_e^3 \rangle / u^{*3} \sim La_{SL}^{-2}$

LES of wide variations in wind & wave forcing

BUT not much inertial shear.

## Kantha & Clayson (2004) model:

$$\frac{Dq^2}{Dt} - \frac{\partial}{\partial x_k} \left[ qlS_q \frac{\partial q^2}{\partial x_k} \right] = 2 \left[ -\overline{u'_i u'_j} \left( \frac{\partial \bar{u}_i}{\partial x_j} + \frac{\partial u_i^S}{\partial x_i} \right) - \beta g_j \overline{u'_j \theta'} - \frac{q^2}{B_1 l} \right]$$

Vortex force production added to M-Y of Kantha & Clayson (1994)

$$\frac{Dq^2 l}{Dt} - \frac{\partial}{\partial x_k} \left[ qlS_l \frac{\partial q^2 l}{\partial x_k} \right] = -E_1 l \overline{u'_i u'_j} \left( \frac{\partial \bar{u}_i}{\partial x_j} + \frac{\partial u_i^S}{\partial x_i} \right) - E_3 l \beta g_j \overline{u'_j \theta'} - \frac{q^3}{B_1} \left( 1 + E_2 \left( \frac{l}{\kappa_w} \right)^2 \right)$$

$$\overline{w' \theta'} = -\overset{\mathbf{K}_H}{S_H} ql \frac{\partial \bar{\theta}}{\partial z}, \quad \overline{v' w'} = -\overset{\mathbf{K}_M}{S_M} ql \frac{\partial \bar{v}}{\partial z}$$

$$S_H = \frac{A_2 (1 - 6A_1 / B_1)}{1 - 3A_2 G_H (6A_1 + B_2 (1 - C_3))}$$

$$S_M = A_1 \frac{(1 - 6A_1 / B_1 - 3C_1) + 9(2A_1 + A_2 (1 - C_2)) S_H G_H}{1 - 9A_1 A_2 G_H}$$

Stability functions

$$G_H = -\frac{l^2}{q^2} \beta g \frac{\partial \theta}{\partial z}, \quad G_M = \frac{l^2}{q^2} \left| \frac{\partial \bar{u}}{\partial z} \right|^2, \quad S_l = S_q = S_H, \quad A_i, B_i, C_i, E_i = \text{const}$$

**Problem: Stability functions do not depend on CL forcing.**

## Equilibrium model, dropping all transport divergence & Coriolis terms:

$$\overline{u'^2} = q^2(1 - 6A_1/B_1)/3 - 6A_1 l q^{-1} \overline{u'w'} \partial_z \overline{u}, \quad \overline{v'^2} = q^2(1 - 6A_1/B_1)/3 - 6A_1 l q^{-1} \overline{v'w'} \partial_z \overline{v}$$

$$\overline{w'^2} = q^2(1 - 6A_1/B_1)/3 + 6A_1 l q^{-1} \left[ \beta g \overline{w'\theta'} - \overline{u'w'} \partial_z u^S - \overline{v'w'} \partial_z v^S \right]$$

$$\overline{v'w'} = -3A_1 l q^{-1} \left[ \left( \overline{w'^2} - C_1 q^2 \right) \partial_z \overline{v} - \beta g \overline{v'\theta'} + \overline{v'^2} \partial_z v^S + \overline{u'v'} \partial_z u^S \right]$$

$$\overline{v'\theta'} = -3A_2 l q^{-1} \left[ \overline{v'w'} \partial_z \overline{\theta} + (1 - C_2) \overline{w'\theta'} \partial_z \overline{v} \right]$$

$$\overline{u'v'} = -3A_1 l q^{-1} \left[ \overline{u'w'} \partial_z \overline{v} + \overline{v'w'} \partial_z \overline{u} \right], \quad \overline{\theta'^2} = -B_2 l q^{-1} \overline{w'\theta'} \partial_z \overline{\theta}$$

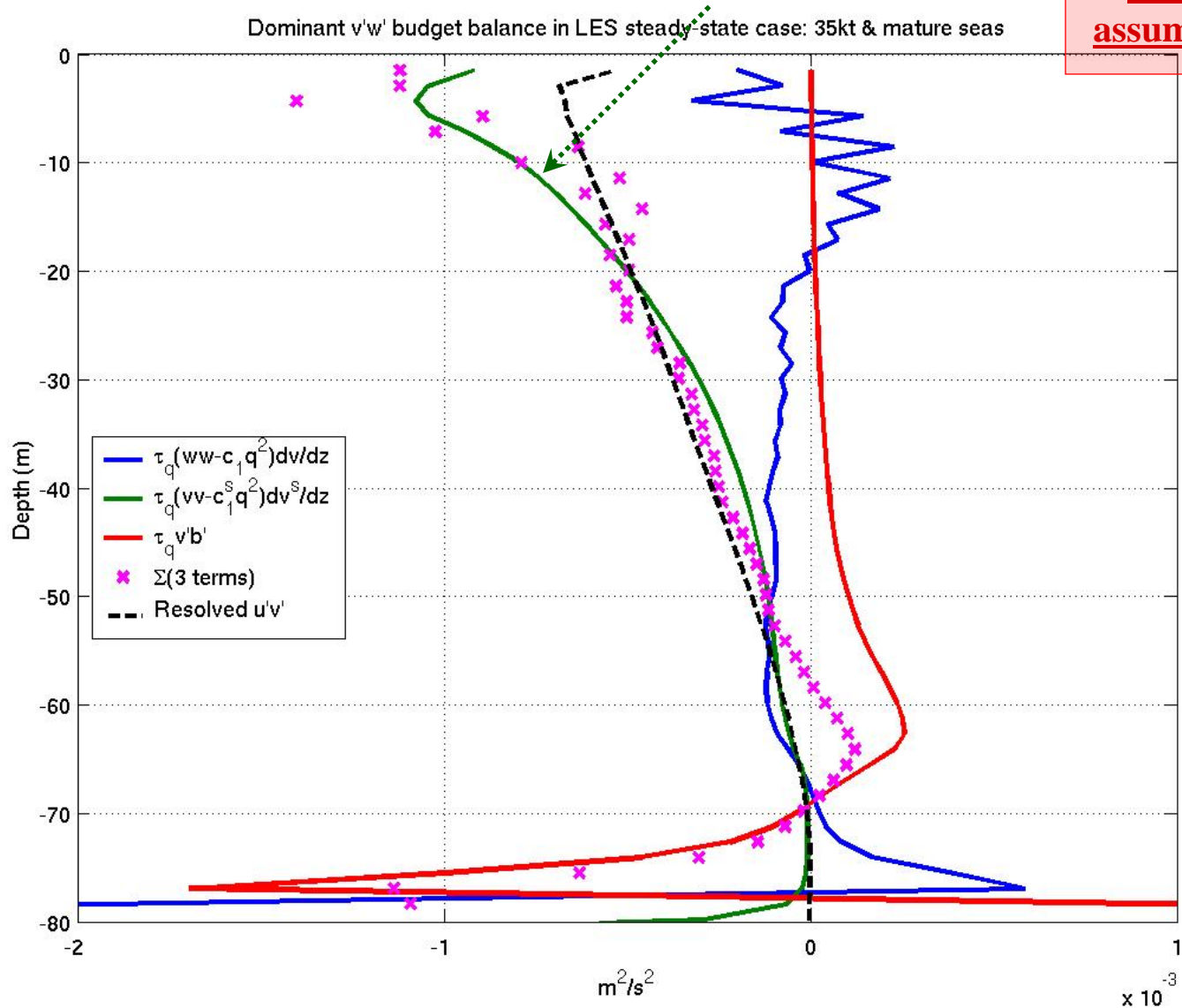
**Solution requires momentum flux down Stokes gradient!**

$$\overline{u'w'} = -lq \left( S_M \partial_z \overline{u} + \underline{S_M^S} \partial_z u^S \right), \quad \overline{v'w'} = -lq \left( S_M \partial_z \overline{v} + \underline{S_M^S} \partial_z v^S \right), \quad \overline{w'\theta'} = -lq S_H \partial_z \overline{\theta}$$

LES  
check:

$$\overline{v'w'} = \underbrace{-3A_1 l q^{-1} \left[ (\overline{w'^2} - C_1 q^2) \partial_z \bar{v} - \beta g \overline{v'\theta'} + (\overline{v'^2} - C_1 q^2) \partial_z v^S + \overline{u'v'} \partial_z u^S \right]}_{\text{time scale } \tau_q} \quad \underbrace{\left[ (\overline{v'^2} - C_1 q^2) \partial_z v^S + \overline{u'v'} \partial_z u^S \right]}_{\text{Dominant term}}$$

**Additional  
closure  
assumption**



**Solution:**  $\overline{u'w'} = -lq(S_M \partial_z \bar{u} + S_M^S \partial_z u^S)$ ,  $\overline{v'w'} = -lq(S_M \partial_z \bar{v} + S_M^S \partial_z v^S)$ ,  $\overline{w'\theta'} = -lqS_H \partial_z \bar{\theta}$

$$S_H = \frac{D_{H0}D_{M1}D_{S1} + D_{H2}D_{M0}D_{S1} + (D_{H3}D_{M1} + D_{M3}D_{H2})D_{S0}}{D_{H1}D_{M1}D_{S1} - D_{H2}D_{M2}D_{S1} - (D_{H3}D_{M1} + D_{M3}D_{H2})D_{S2}}$$

$$S_M^S = (D_{S0} + D_{S2}S_H)/D_{S1}, \quad S_M = (D_{M0} + D_{M2}S_H + D_{M3}S_M^S)/D_{M1}$$

**Stability functions: Much more complicated!!**

$$D_{S0} = A_1(1 - 6A_1/B_1 - 3C_1^S), \quad D_{S1} = 1 - 9A_1(A_2G_H + A_1G_V), \quad D_{S2} = 9A_1A_2C_2^S G_H$$

$$D_{M0} = A_1(1 - 6A_1/B_1 - 3C_1), \quad D_{M1} = 1 - 9A_1(A_2G_H + 4A_1G_V),$$

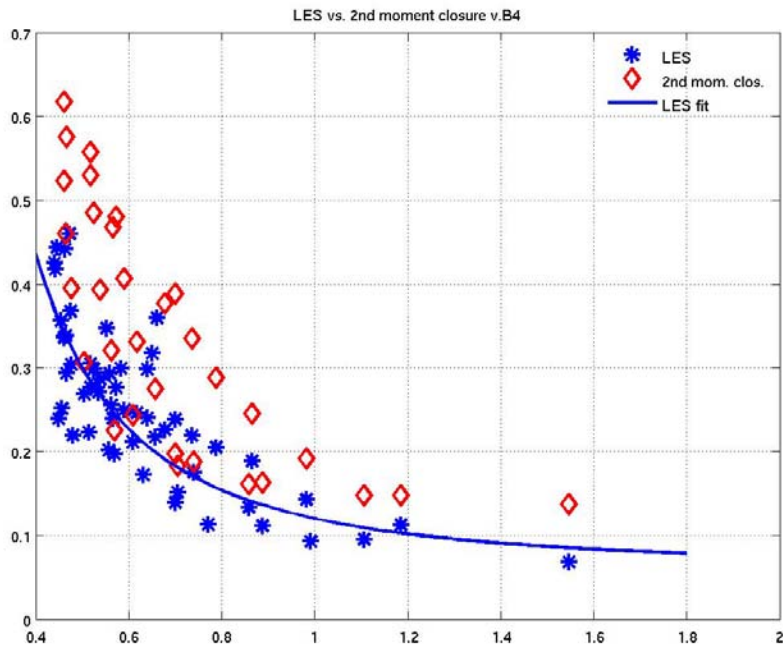
$$D_{M2} = 9A_1(2A_1 + A_2(1 - C_2))G_H, \quad D_{M3} = 27A_1^2 G_S$$

$$D_{H0} = A_2(1 - 6A_1/B_1), \quad D_{H1} = 1 - 3A_2 \left[ (6A_1 + B_2(1 - C_3))G_H + 3A_2(1 - C_2)G_V - 3A_2C_2^S G_S \right],$$

$$D_{H2} = 9A_2G_V(2A_1 + A_2), \quad D_{H3} = 9A_2G_S(2A_1 + A_2)$$

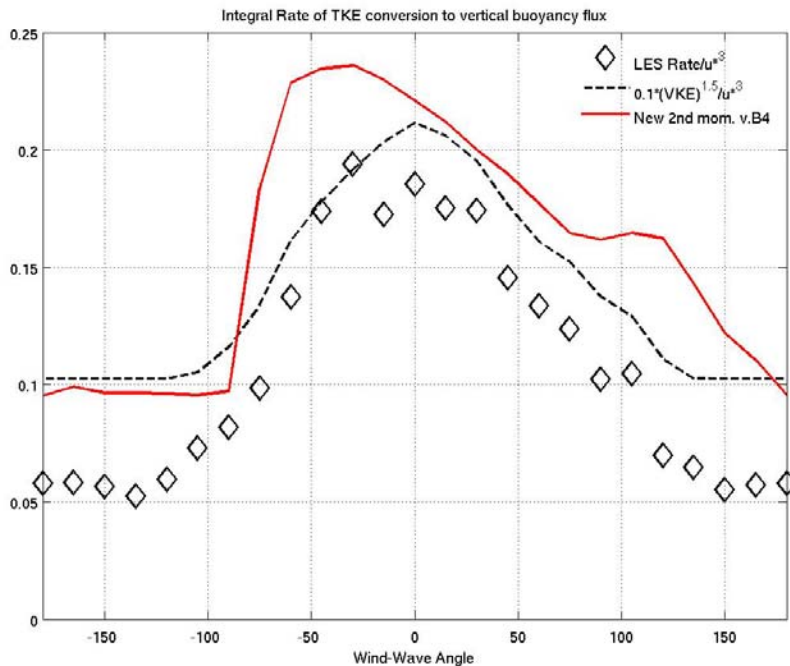
**New n.d. forcing functions**

$$G_H = -\frac{l^2}{q^2} \beta g \frac{\partial \theta}{\partial z}, \quad G_M = \frac{l^2}{q^2} \left| \frac{\partial \vec{u}}{\partial z} \right|^2, \quad G_V = \frac{l^2}{q^2} \frac{\partial \vec{u}}{\partial z} \cdot \frac{\partial \vec{u}^S}{\partial z}, \quad G_S = \frac{l^2}{q^2} \left| \frac{\partial \vec{u}^S}{\partial z} \right|^2$$



Entrainment power scaling: LES vs. closure:

Corresponding scaling of work rate with  $La_{SL}$  -- Closure model entrainment higher overall.



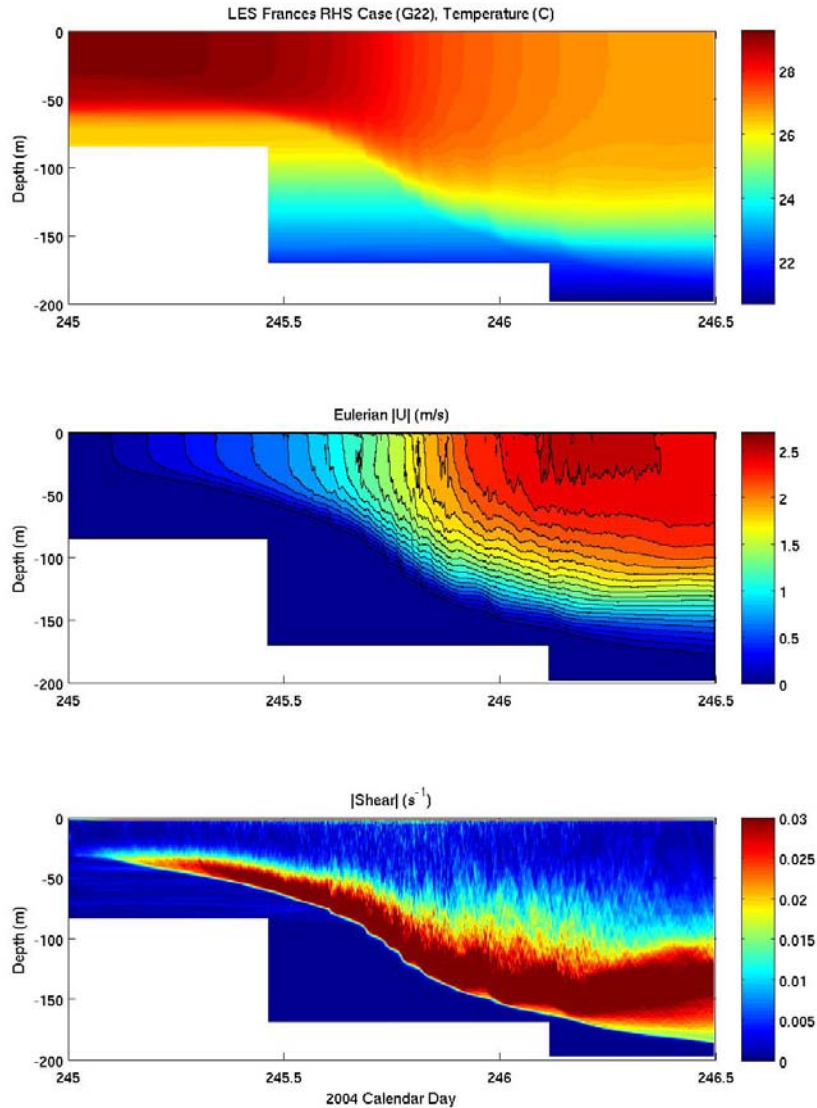
Similar response to angle between wind & waves -- skewness from Coriolis stronger.



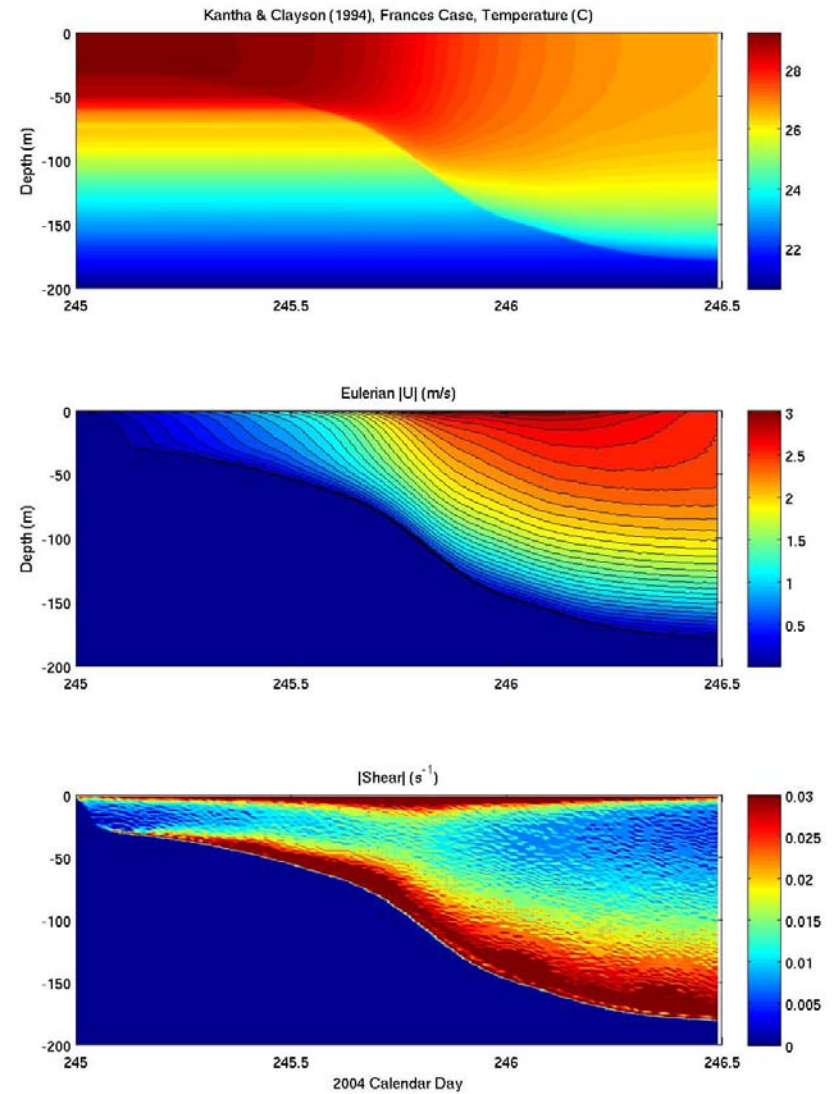
# LES vs 2<sup>nd</sup> moment M-Y closure (Kantha & Clayson, 1994), i.e. NCOM

## Wave forcing from WW3 model (by Il-Ju Moon)

### LES

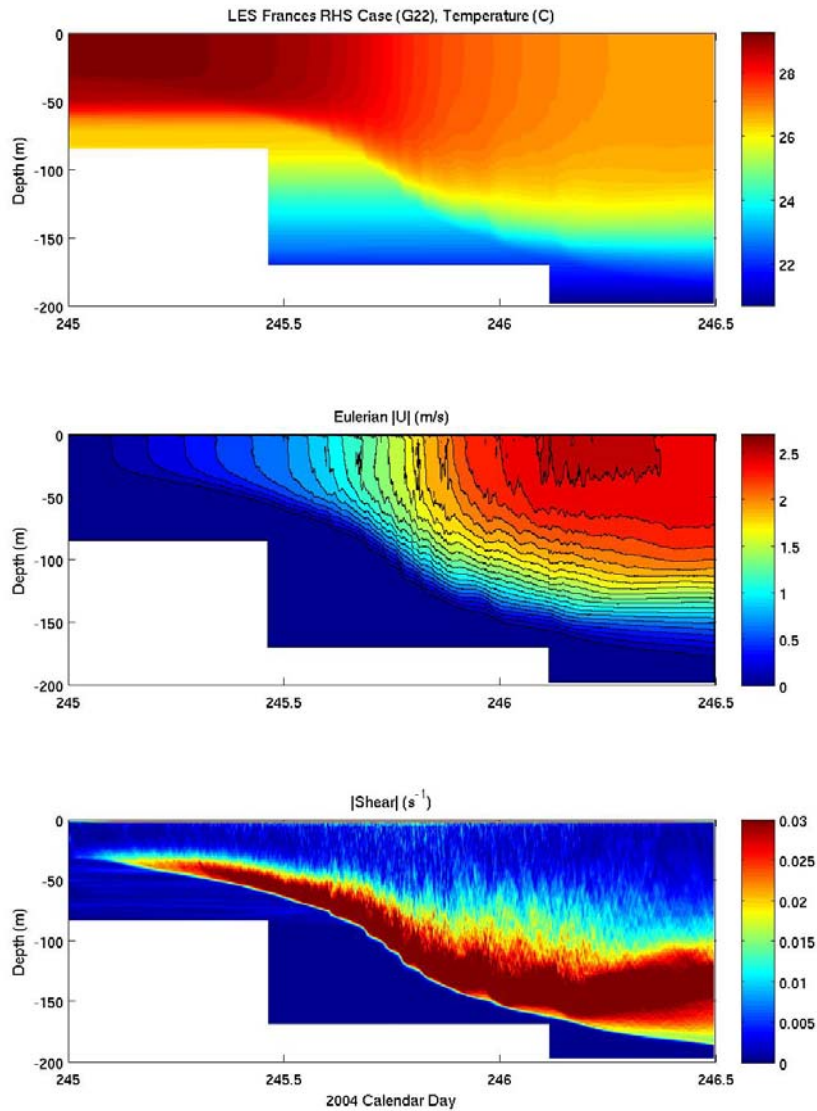


### Kantha & Clayson (1994)

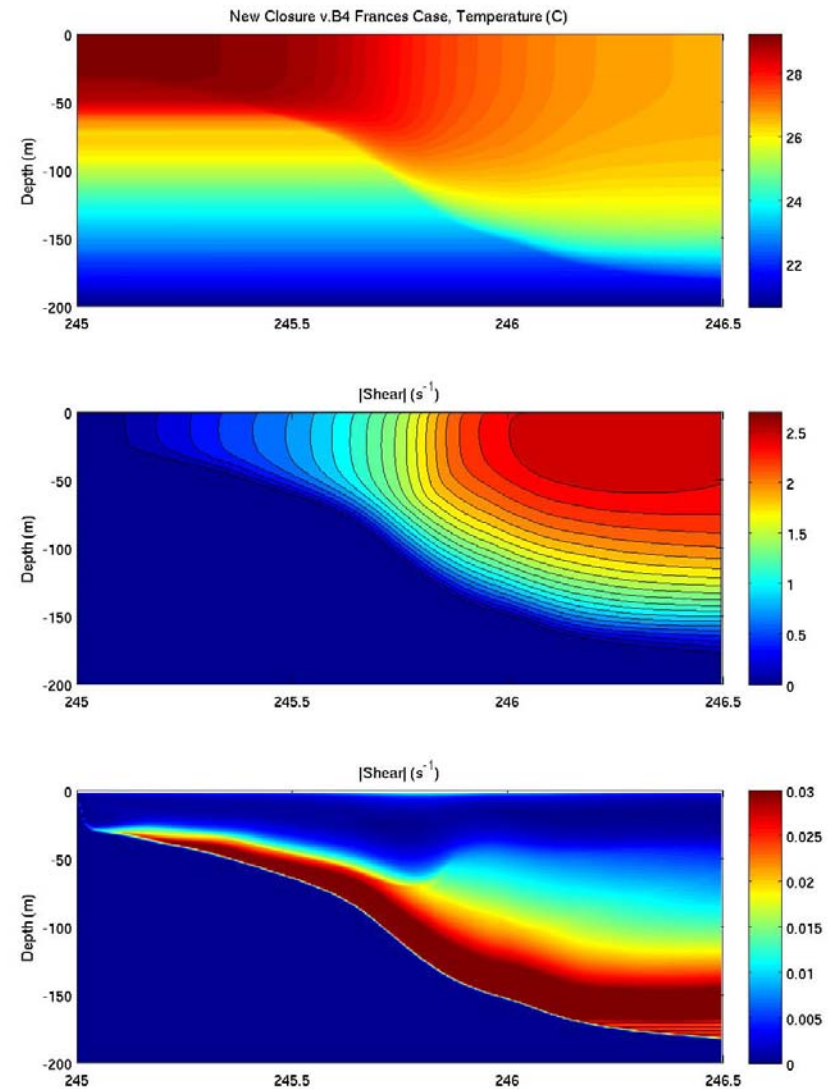


# LES vs recent new 2<sup>nd</sup> moment closure

## LES



## New 2<sup>nd</sup> moment closure v.B4



## Entrainment physics across cyclone:

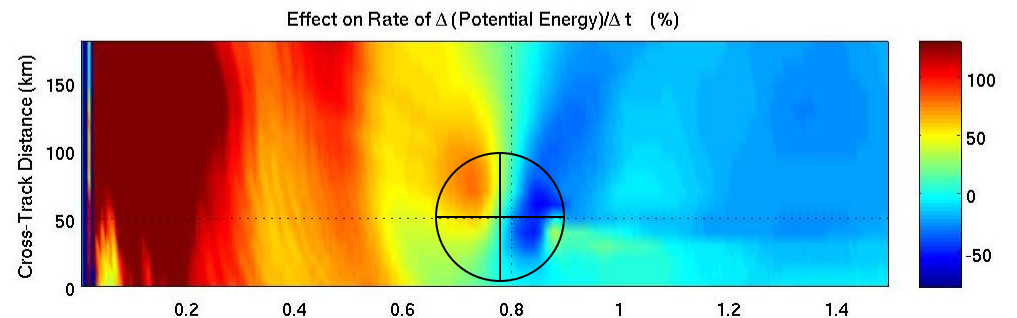
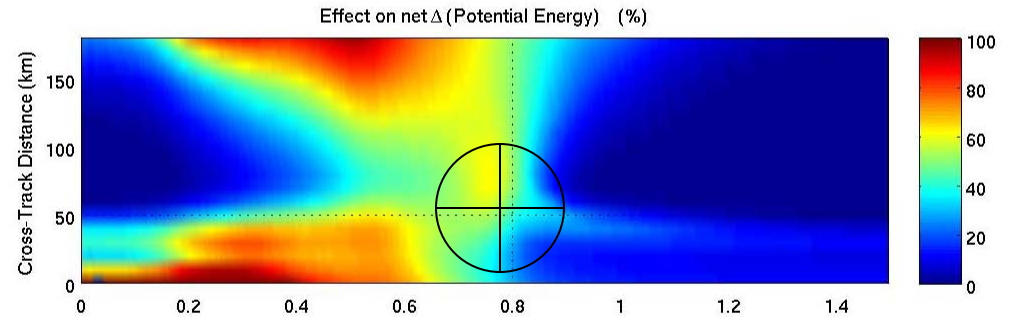
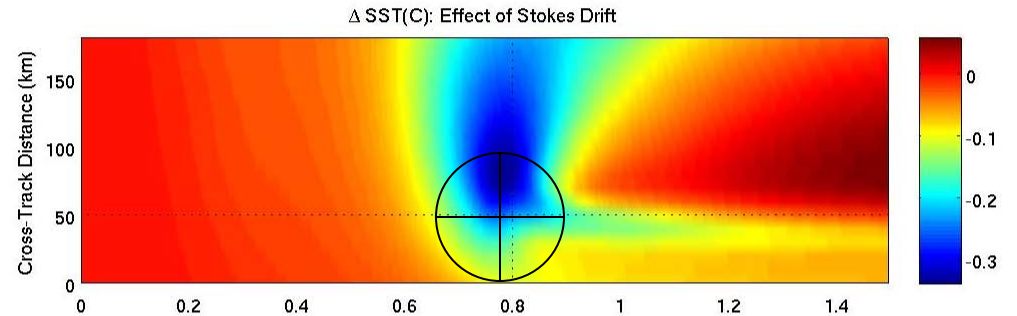
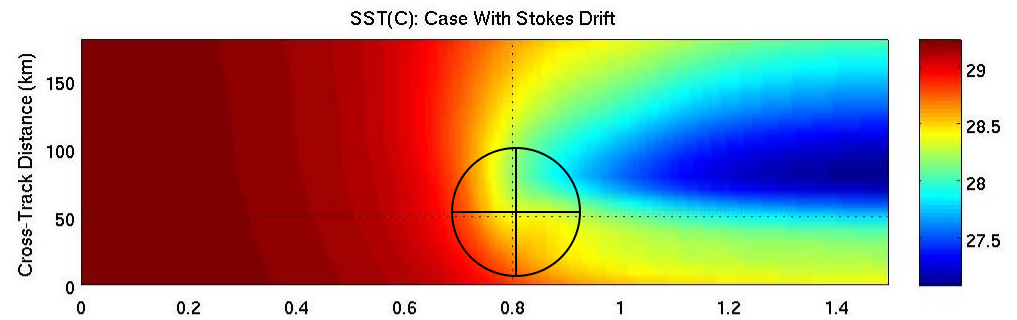
Final wake formation dominated by mixing driven by inertial shear.

Intermediate state, timing of wake below cyclone shifted by Stokes drift.

Below maximum winds, cooling is 50% more: reduced 1 C vs 2/3 C .

Mixing enhanced ahead of cyclone, damped to rear.

Combined effects cancel and are also much less than shear-driven mixing.



## Entrainment physics across cyclone:

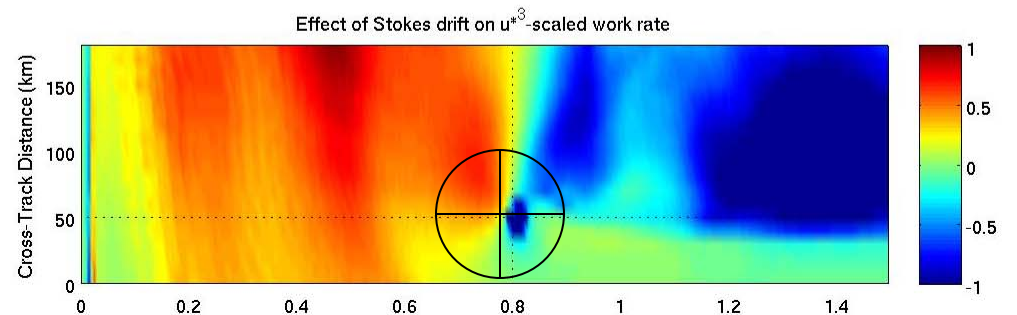
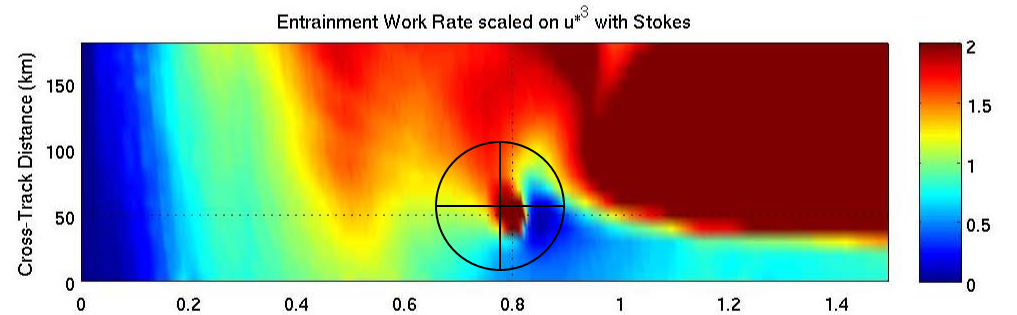
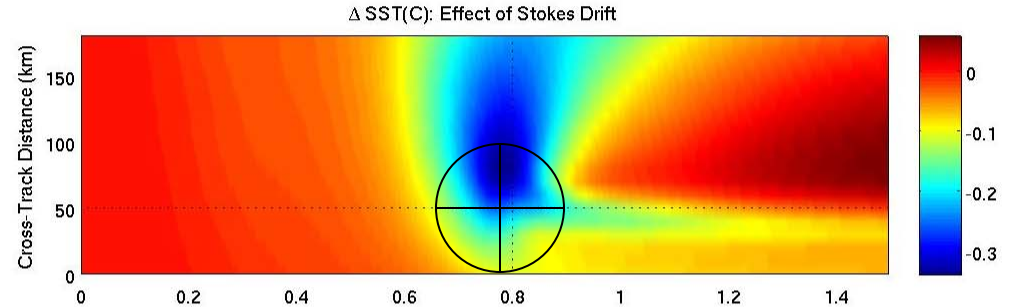
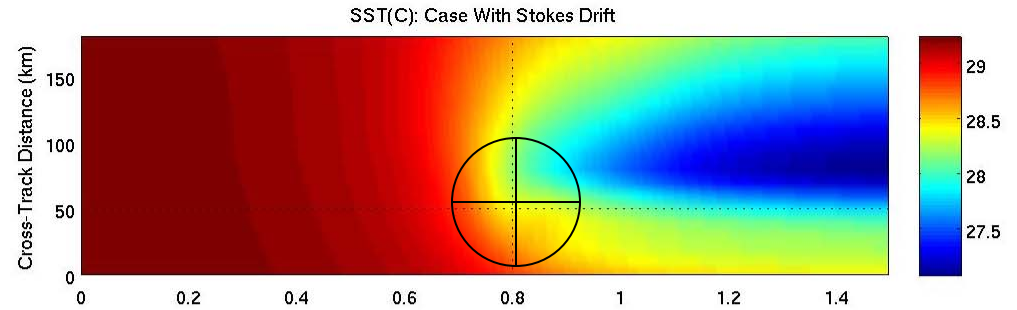
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Wave-modified turbulence closure and LES (P. Sullivan too) need wind & wave forcing from Typhoons to simulate ITOP turbulence observations. Best: archived wave model data (WW3, SWAN) verified against remote & in-situ observations.

Seeking collaboration to put into modified closure in wave-ocean coupled model.

Lots of SST, Ocean Color imagery prepared for field cruise operations in small geographic domains still available at [itop.org/data/harcourt](http://itop.org/data/harcourt) . Includes some daily AVISO maps -- AVISO archives weekly maps. Other original satellite data archived at NODC & others, so .... should we archive any of this imagery?



